Theoretical Study - Long Range on LiH₂

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Introduction

The lithium chemistry has received a great attention in recent years due to the importance that LiH molecules and its ionic variants can have in the primordial universe [1,2]. The reaction LiH + H \rightarrow Li + H₂ is considered to contribute to LiH depletion, while the hydrogen-exchange reaction LiH + H \rightarrow LiH + H leads to the retention of LiH in this process.

In this work we report our recent studies on the long-range interactions between the reactants of those reactions. For the LiHH system, the main contribution for the long-range interactions is the dispersion interaction. To modeling the dispersion interaction, the parallel and perpendicular values of the polarizabilities, a, for the diatomics (H-H and Li-H) have been calculated and fitted using the follow equation (see figure).

$$F(R) = A + \left(\sum_{i=0}^{3} B_i R^i\right) \exp\left(-\sum_{i=1}^{3} C_i R^i\right) + \left(1 - \exp(-D_3 R^5)\right) E_3 / R^3 + \left(1 - \exp(-D_6 R^8)\right) E_6 / R^6$$

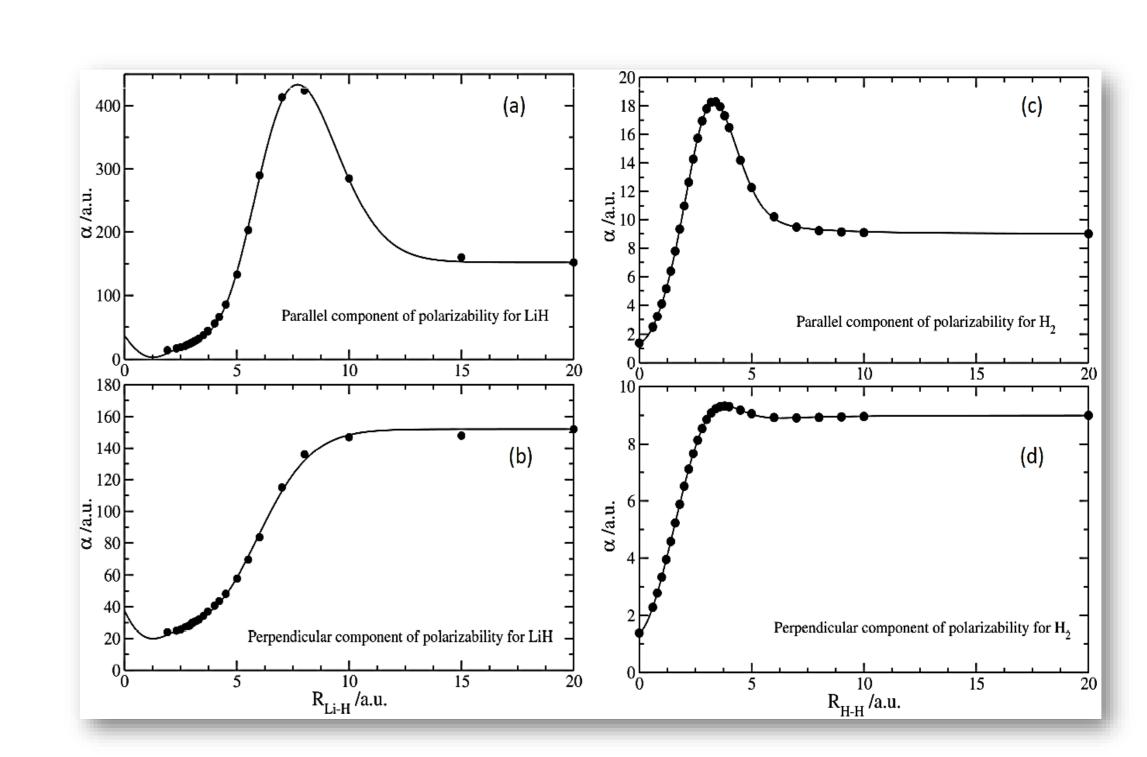


Figure: Parallel and perpendicular components of polarizabilities, α , for LiH ((a) and (b)) and H₂ ((c) and (d)). Solid lines are the functional form fit to the ab initio calculations (solid dots).

Dispersion interaction coefficients

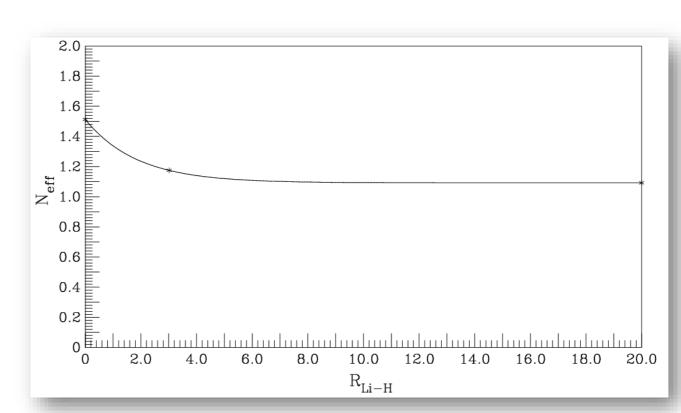
The dispersion interaction coefficients C_6 can then be computed as C_8 and C_{10} have been semiempirically estimated from C_6 using a universal correlation.

We found it convenient to use the follow expression for the variation of Neff with the diatomic distance.

$$N_{eff}(R) = N_{\infty} + [a + b(R - R_e)] \exp[c(R - R_e)]$$

The parameters a, b and c have been defined in order to reproduce the united atom and far apart, N_{∞} , limits as well as an equilibrium value, if known.

 $C_{6}^{\parallel,\perp} (AB - C) (R) = \frac{3}{2} \alpha_{AB}^{\parallel,\perp}(0) (R) \alpha_{C}(0)$ $\times \left[\left(\frac{\alpha_{AB}^{\parallel,\perp}(0) (R)}{N_{eff}^{AB} (R)} \right)^{\frac{1}{2}} + \left(\frac{\alpha_{C}(0)}{N_{eff}^{C}} \right)^{\frac{1}{2}} \right]^{-1}$



To better model the dispersion interaction we need the coefficients Cn (AB - C)(R), n = 8 and 10. When available we have used literature values, otherwise, we have semiempirically estimated those coefficients from C6 using a universal correlation.

$$C_n^{\parallel,\perp} (AB - C) (R) = C_6^{\parallel,\perp} (AB - C) (R) k_n R_0^{[a(n-6)/2]} (AB - C) (R)$$

In lack of accurate values for the Le Roy's parameter, RO(AB - C)(R), we have estimated it using the follow equation, where we use the mean polarizability of the diatomic as a measure of the diatomic volume and the atomic radius is taken from the literature.

$$R_0(AB - C)(R) = 2 \left[\langle \overline{\alpha}_{AB}(0)(R) \rangle^{\frac{1}{3}} + \langle r_C^2 \rangle^{\frac{1}{2}} \right] f_{corr}^n(R)$$

R_{0 H-LiH} LiH(¹Σ)

16.0

14.0

19.0

11.0

10.0

10.0

10.0

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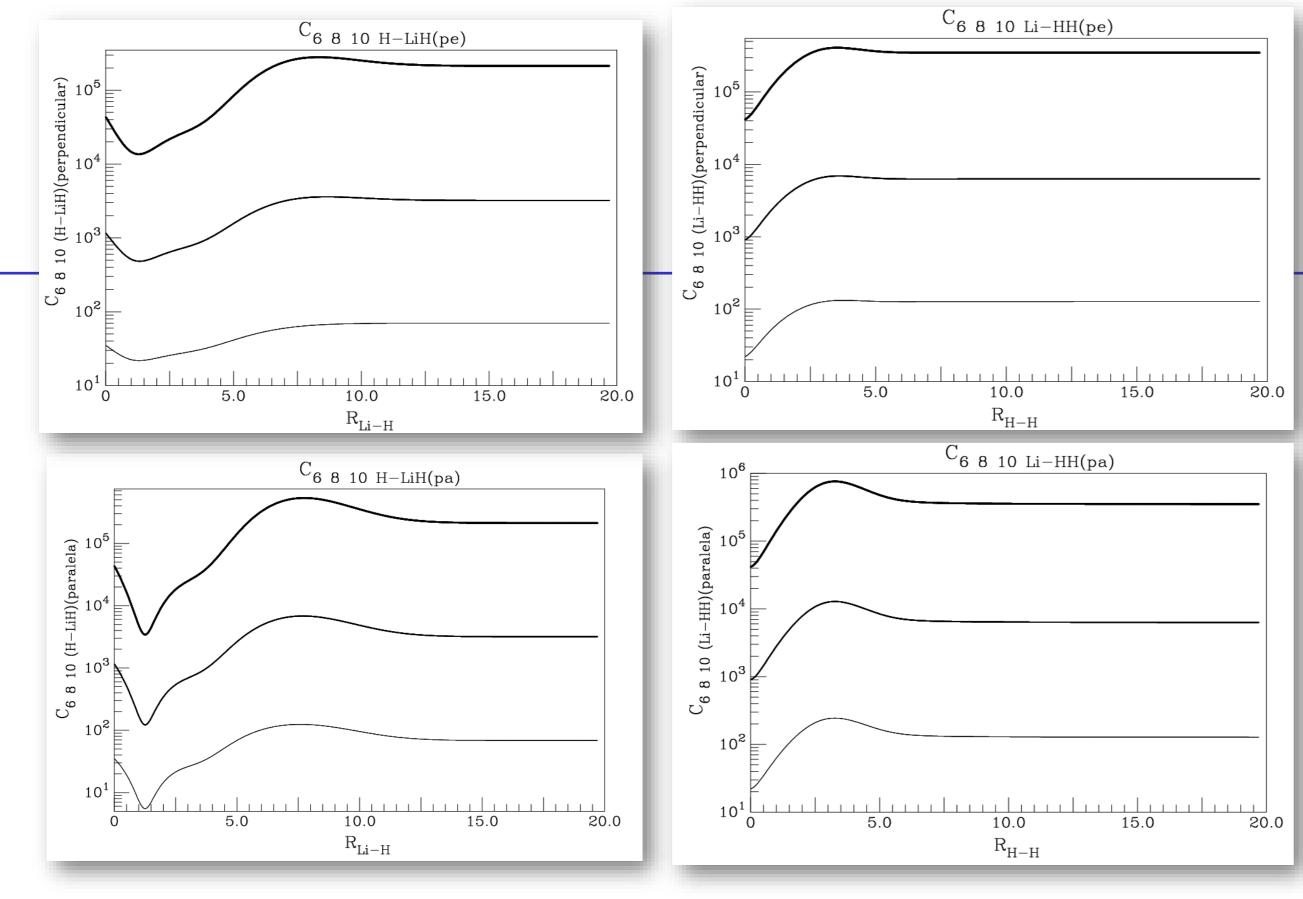
Li - HH

0° (___)

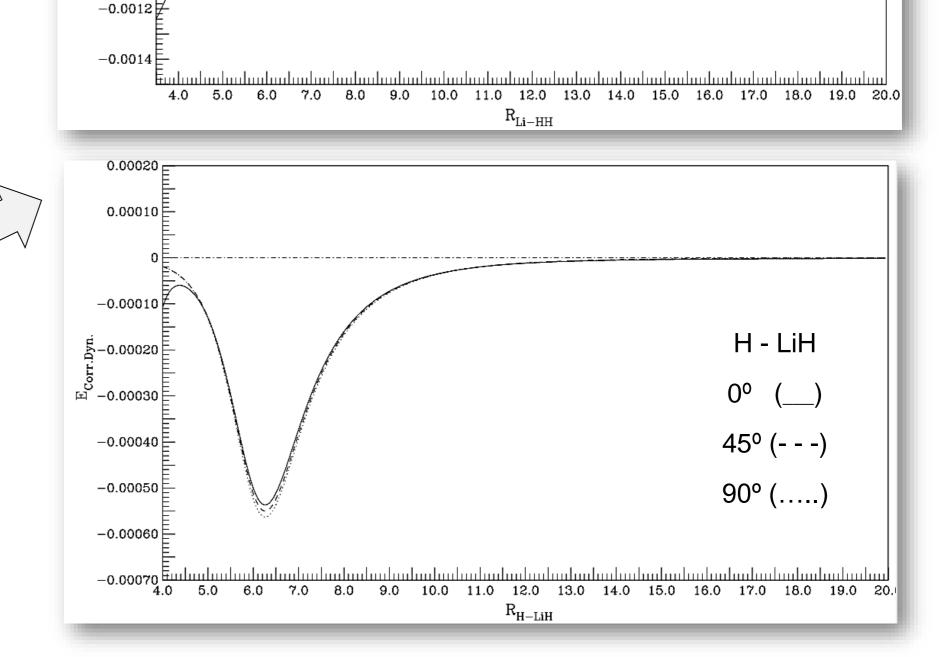
45° (- - -)

90° (....)

The total dispersion interaction will be computed as a function of Cn and inter-atomic distances [3].



 $C_n(R_i, \theta_i) = \frac{1}{3} \left(2 C_n^{\perp}(R) + C_n^{\parallel}(R) \right) + \frac{1}{3} \left(C_n^{\parallel}(R) - C_n^{\perp}(R) \right) \times (3 \cos^2 \theta_i - 1)$



The dynamical correlation energy has been computed using the follow equation.

$$V_{dc} = \sum_{i=1}^{3} S(R_i, r_i) \sum_{n=6}^{10} C_n^i(R_i, \theta_i) \chi_n(r_i) r_i^{-n}$$

$$+ \sum_{i=1}^{3} \left[\prod_{j \neq i} (1 - S(R_j, r_j)^2) \right] \sum_{n=6}^{10} C_n^i \chi_n(R_i) R_i^{-n},$$

The dynamical correlation energy is shown for the interaction Li-HH and H-LiH, at different approaching angles between atom and diatomic molecule 0°, 45° and 90°.

References:

1. S. Lepp, J. Shull, Astrophys. J. **1984**, 280, 465.

-0.0004

분 -0.0006

-0.0008

-0.0010

- 2. A. Dalgarno, S. Leep, S.P. Tarafdar, M.P. Varshni (Eds.), Astrochemistry, Reidel, **1987**.
- 3. João Brandão and Carolina M.A. Rio, Chem. Phys. Lett. 2003, 372, 866.